

للبيانات معادلة الحمل
Fatigue Crack growth rate could be expressed in the form

of empirical relationship: $\frac{dc}{dN} = A T^n$ — (A)

For a single edge notch specimen: $T = 2K_1 C U$

C = crack length, N = number of cycles, T is surface work parameter (analogous to G ~~fracture energy~~ in linear elastic fracture mechanics).

$U = \sigma^2 / 2E$ = the stored energy density for a linear elastic material; K_1 = const. varies from π at small extensions (linear elastic value) to approximately unity (1) at large extensions. A and n constants depend on the material and vary with test conditions such as Temp. n lies between (1-6) and equal to 2 for rubbers.

T is positive quantity vary during the test cycle from zero ($T = T_{min}$) to a finite value ($T = T_{max}$). the const. ~~is~~ if T_{min} ^{is} increased, there is a corresponding decrease in A ;

This attributed to reduced crack propagation where strain induced crystallization occurs.

~~the limiting value $T = T_0$~~

The limiting value $T = T_0$ is called the fatigue limit below ~~which~~ it a fatigue crack will not propagate.

~~The above~~ The above relationship is applicable on rubbers.

For glassy polymers, the fatigue crack growth rate is usually expressed in the form of empirical relationships,

~~the~~
$$\frac{dc}{dN} = A' (\Delta K)^m \quad \text{--- (B)}$$
 c : crack length;

N : number of cycles; ΔK : range of the stress intensity

Factor ($K_{max} - K_{min}$); K_{min} is generally zero.

A' and m are constants depending on the material and test

conditions. (equation (B) is called Paris equation).

Strain energy release rate $G = K^2/E$ for plane stress

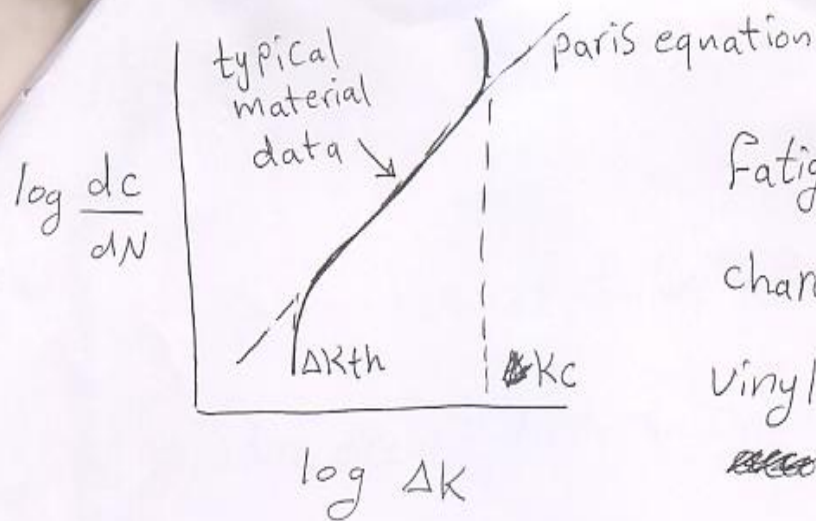
$$G = 2T = K_{max}^2/2E = (\Delta K)^2/2E$$

A and B equation are identical if $K_{min} = 0$ and equivalent

if $m = 2n$; equation B is applied for predicting fatigue

crack growth rates in metals.

The following figure is represented Paris equation



Fatigue crack growth characteristics for a vinyl urethane polymer

ΔK_{th} = threshold value of ΔK , below which no crack growth is observed, as ΔK approaches the critical stress intensity factor K_c , the crack accelerates.

There is a strong sensitivity ^{between} ~~of~~ fatigue crack growth and molecular weight.

For example: in PS a five fold increase in molecular weight resulted in a more than 10-fold increase in fatigue life.